

# An Introduction to Automated Program Verification with Permission Logics



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# Initial Example (Pseudo Java)

---

```
class Cell {  
    int v  
  
    void add(Cell c)  
    { v = v + c.v }  
}
```

---

```
void client() {  
    Cell c1 = new Cell()  
    c1.v = 1  
    Cell c2 = new Cell()  
    c2.v = 2  
  
    c1.add(c2)  
  
    assert c1.v == 3  
    assert c2.v == 2  
}
```

---

Goal: Check assertions **statically**

Challenges:

- Whole-code analysis is **expensive**
- **Dynamic dispatch** (inheritance; open-world assumption)

# Modularity


---

```
class Cell {  
    int v  
  
    void add(Cell c)  
    { ██████████ }  
}
```

---

```
void client() {  
    Cell c1 = new Cell()  
    c1.v = 1  
    Cell c2 = new Cell()  
    c2.v = 2  
  
    c1.add(c2)  
  
    assert c1.v == 3  
    assert c2.v == 2  
}
```

---



# Specifications

---

```
class Cell {  
    int v  
  
    void add(Cell c)  
        requires c != null  
        ensures v == old(v) + old(c.v)  
    { v = v + c.v }  
}
```

---

---

```
void client() {  
    Cell c1 = new Cell()  
    c1.v = 1  
    Cell c2 = new Cell()  
    c2.v = 2  
  
    c1.add(c2)  
  
    assert c1.v == 3  
    assert c2.v == 2  
}
```

---

# Reasoning with Specifications

---

```
class Cell {  
    int v  
  
    void add(Cell c)  
        requires c != null  
        ensures v == old(v) + old(c.v)  
    { ██████████ }  
}
```

---

---

```
void client() {  
    Cell c1 = new Cell()  
    c1.v = 1  
    Cell c2 = new Cell()  
    c2.v = 2  
  
    c1.add(c2)  
  
    assert c1.v == 3  
    assert c2.v == 2  
}
```


---



# An Incorrect Implementation

---


```
class Cell {  
    int v  
  
    void add(Cell c)  
        requires c != null  
        ensures v == old(v) + old(c.v)  
    {  
        v = v + c.v  
        c.v = 0  
    }  
}
```



---

---


```
void client() {  
    Cell c1 = new Cell()  
    c1.v = 1  
    Cell c2 = new Cell()  
    c2.v = 2  
  
    c1.add(c2)  
  
    assert c1.v == 3  
    assert c2.v == 2  
}
```



---

# Strengthening Specifications

---

```
class Cell {  
    int v  
  
    void add(Cell c)  
        requires c != null  
        ensures v == old(v) + old(c.v)  
        ensures c.v == old(c.v)   
    {  
        v = v + c.v  
        c.v = 0  
    }  
}
```

---

---

```
void client() {  
    Cell c1 = new Cell()  
    c1.v = 1  
    Cell c2 = new Cell()  
    c2.v = 2  
  
    c1.add(c2)  
  
    assert c1.v == 3  
    assert c2.v == 2  
}
```

---

# Strengthening Specifications

---

```
class Cell {  
  int v  
  
  void add(Cell c)  
    requires c != null  
    ensures v == old(v) + old(c.v)  
    ensures c.v == old(c.v) ?  
    { v = v + c.v }  
}
```

---

---

```
void client() {  
  Cell c1 = new Cell()  
  c1.v = 1  
  Cell c2 = new Cell()  
  c2.v = 2  
  
  c1.add(c2)  
  
  assert c1.v == 3  
  assert c2.v == 2  
}
```

---



# Aliasing

---

```
class Cell {  
  int v  
  
  void add(Cell c)  
    requires c != null  
    ensures v == old(v) + old(c.v)  
    ensures c.v == old(c.v) X  
  { v = v + c.v }  
}
```

---

```
void client() {  
  Cell c1 = new Cell()  
  c1.v = 1  
  Cell c2 := new Cell()  
  c2.v = 2
```

█ c1.add(c1)

assert c1.v == 3 X

assert c2.v == 2 X

}

## Challenges

**Reason about Shared State  
(Including Data Races)**

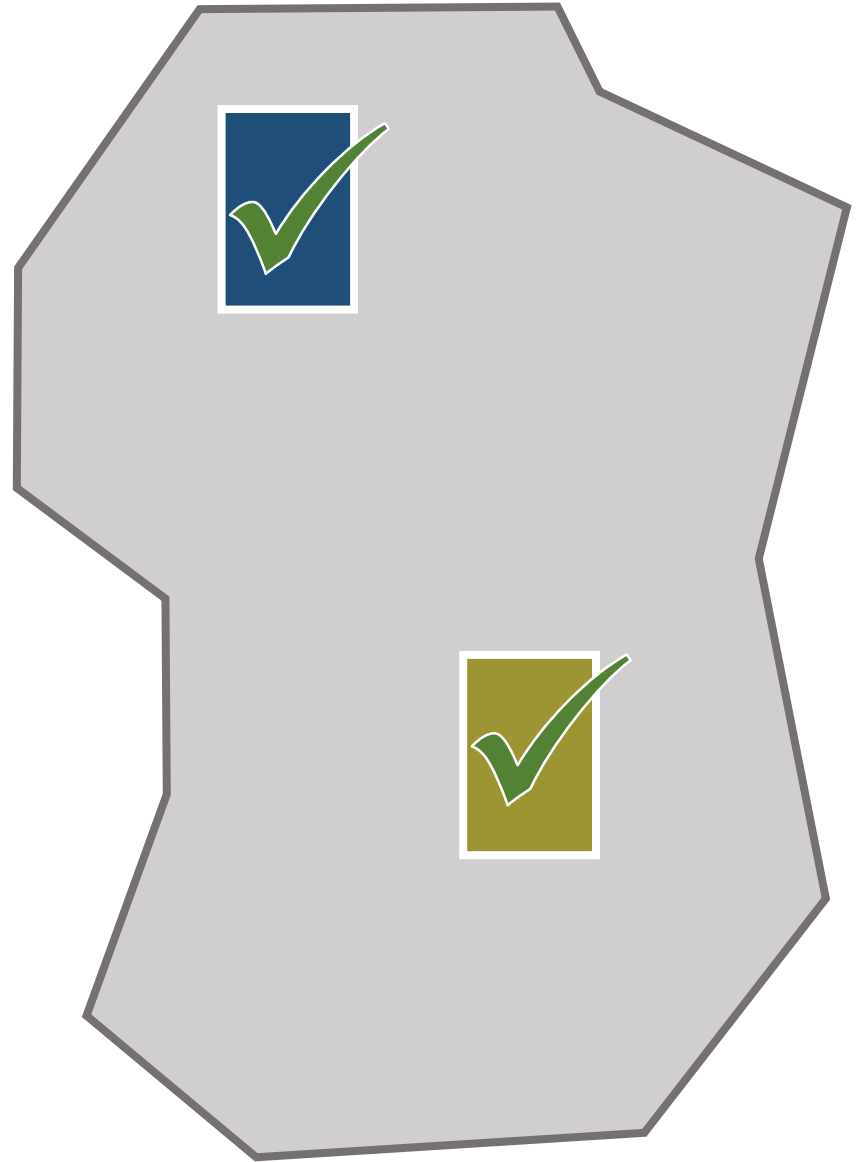
**and**

**Control Aliasing**

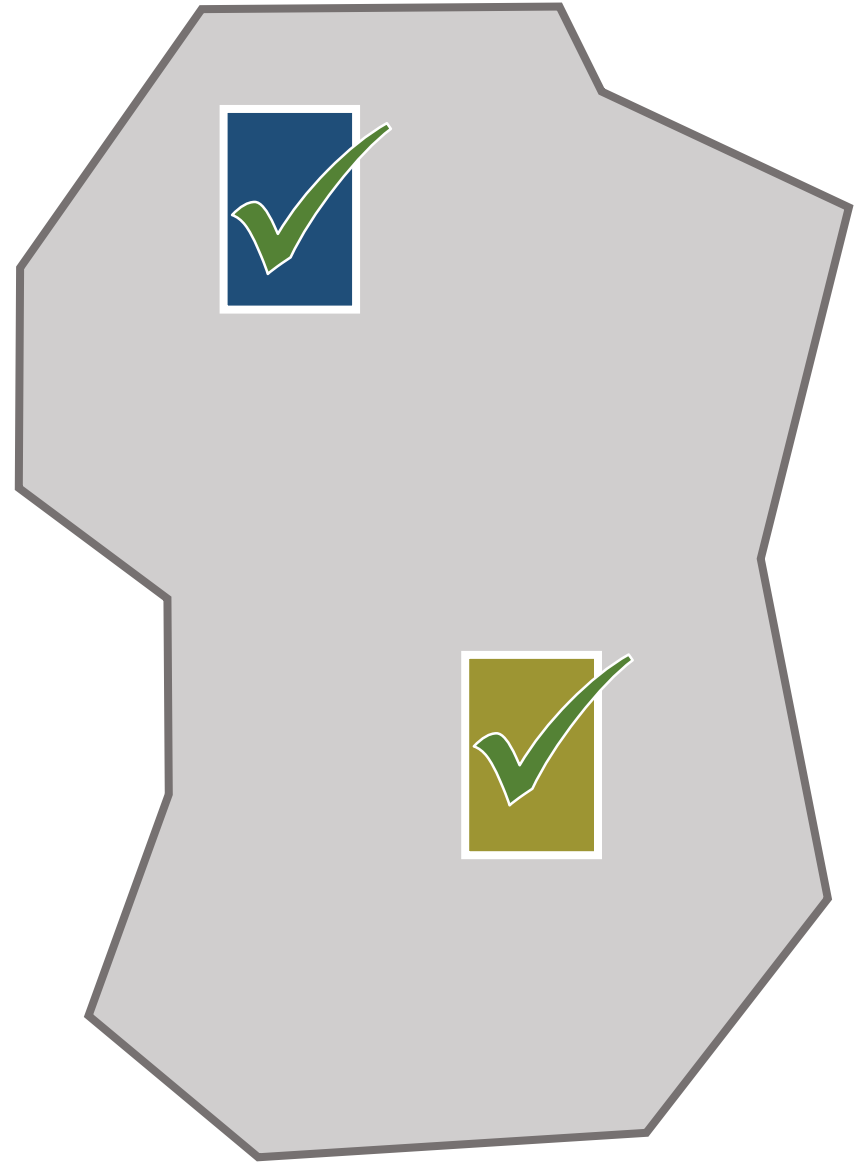
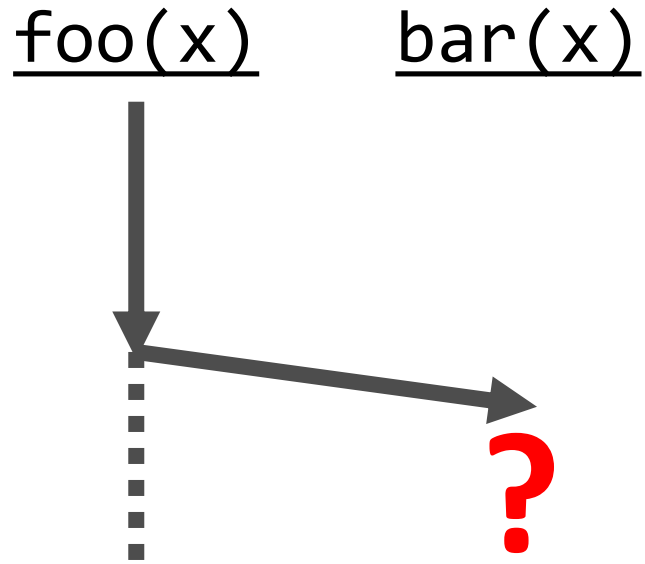
# Modular Static Verification + Shared State

foo(x)

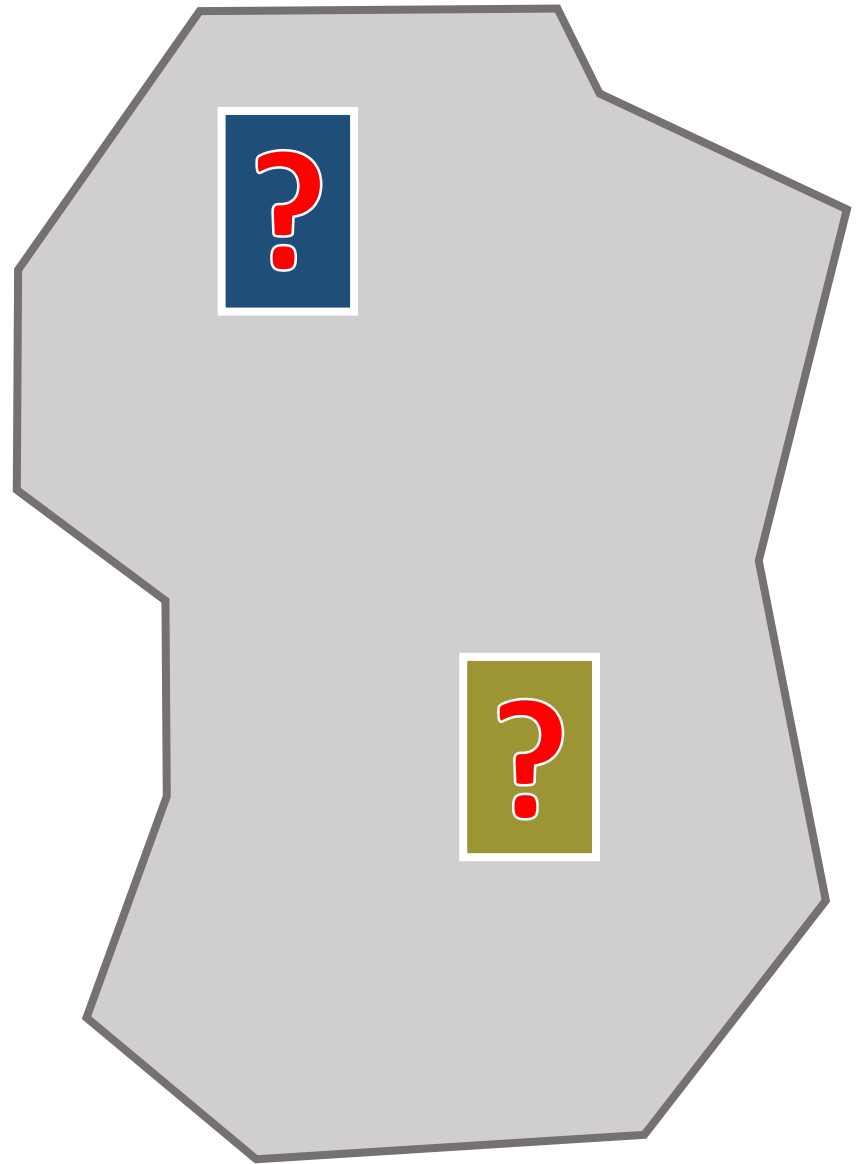
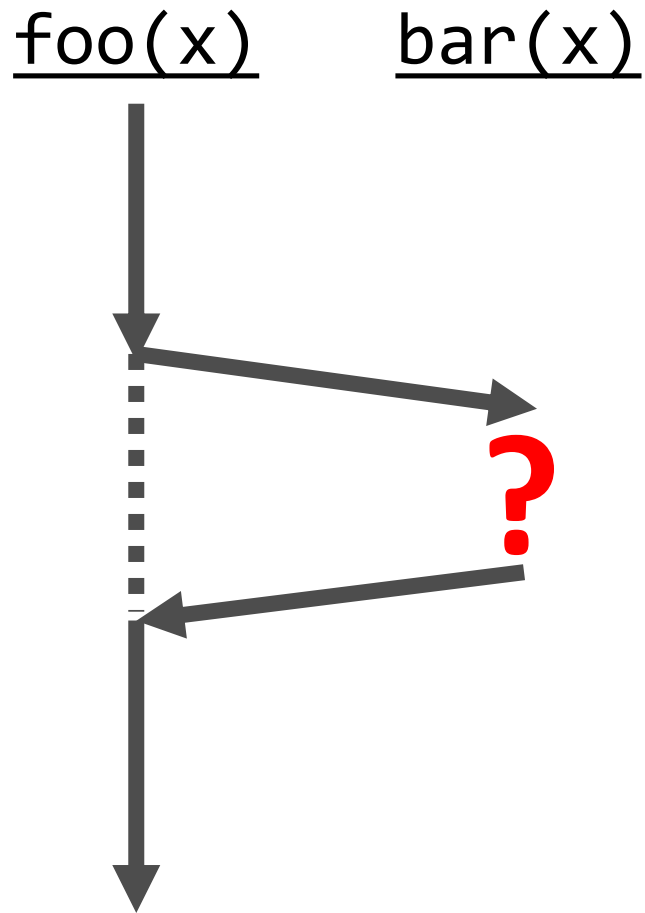
bar(x)



# Modular Static Verification + Shared State



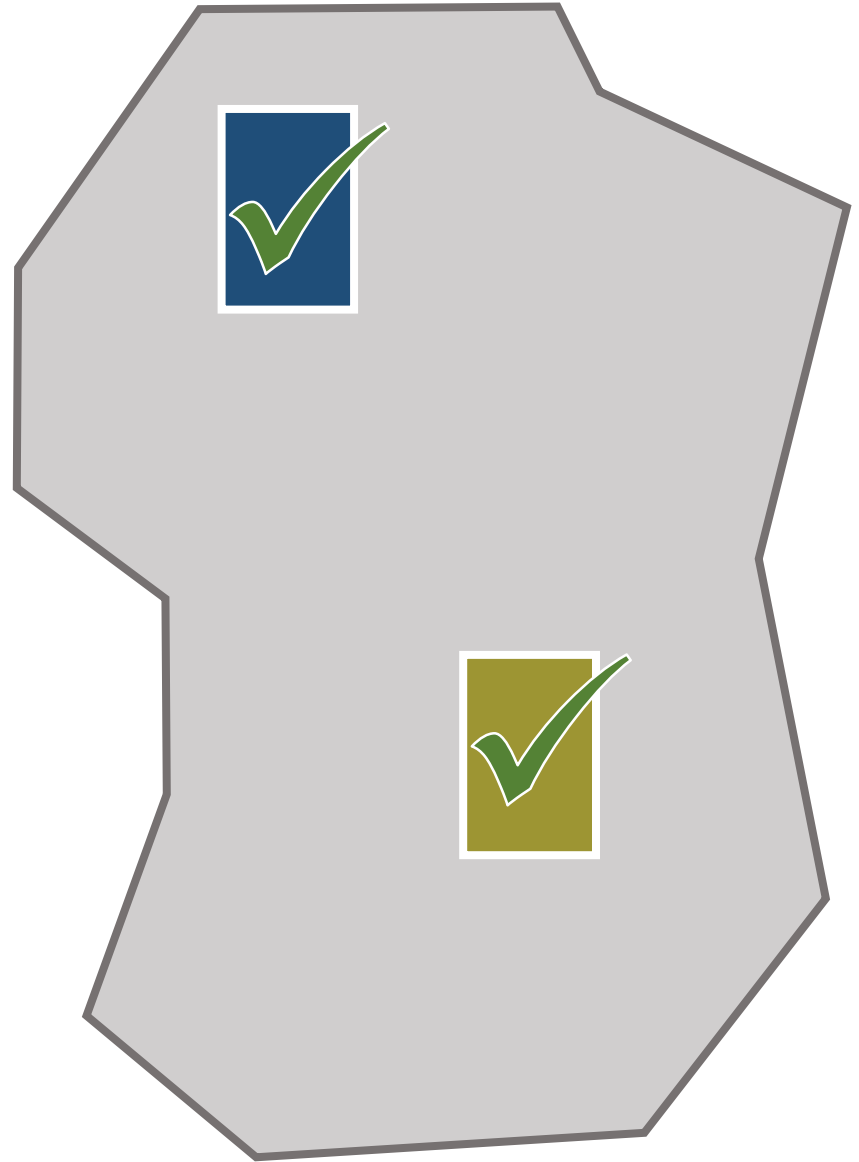
# Modular Static Verification + Shared State



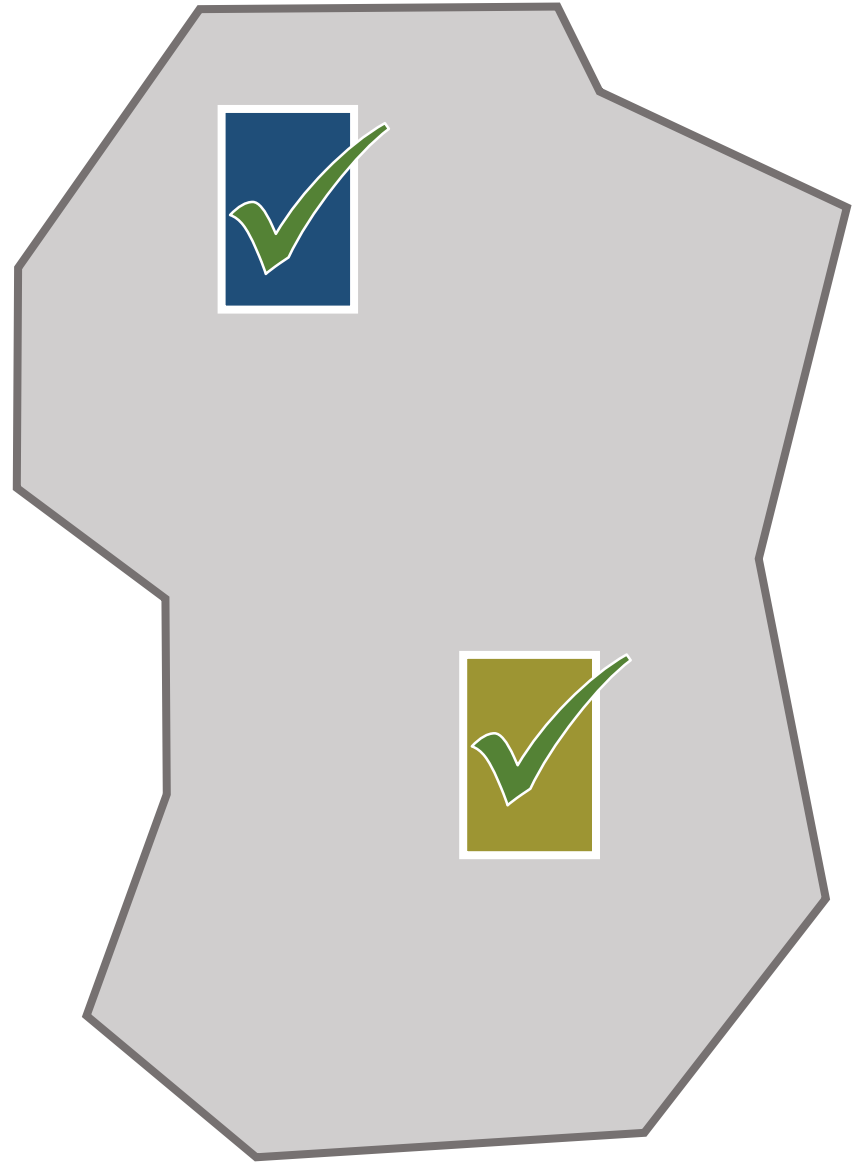
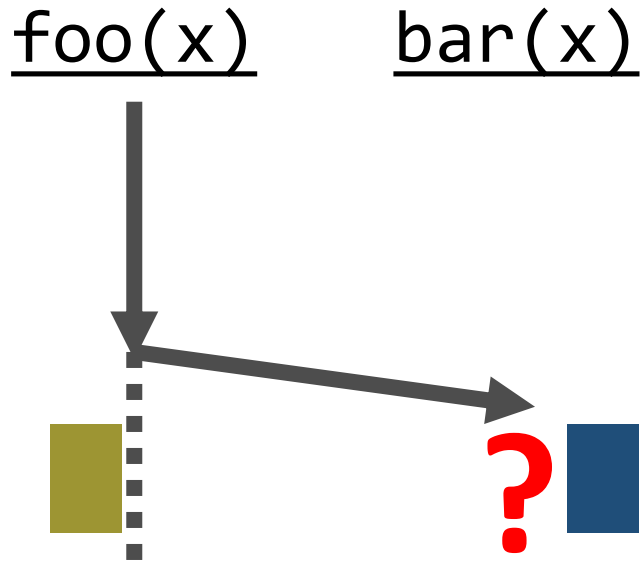
# Permissions

foo(x)

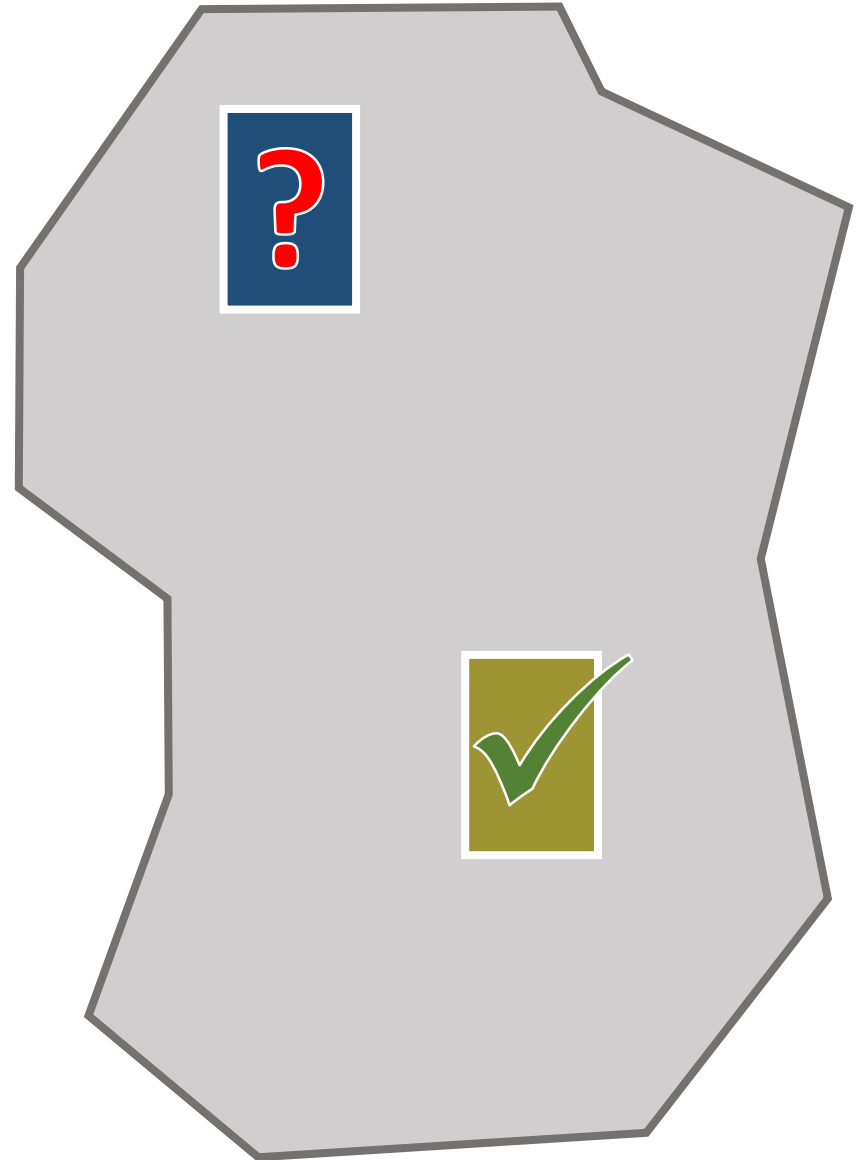
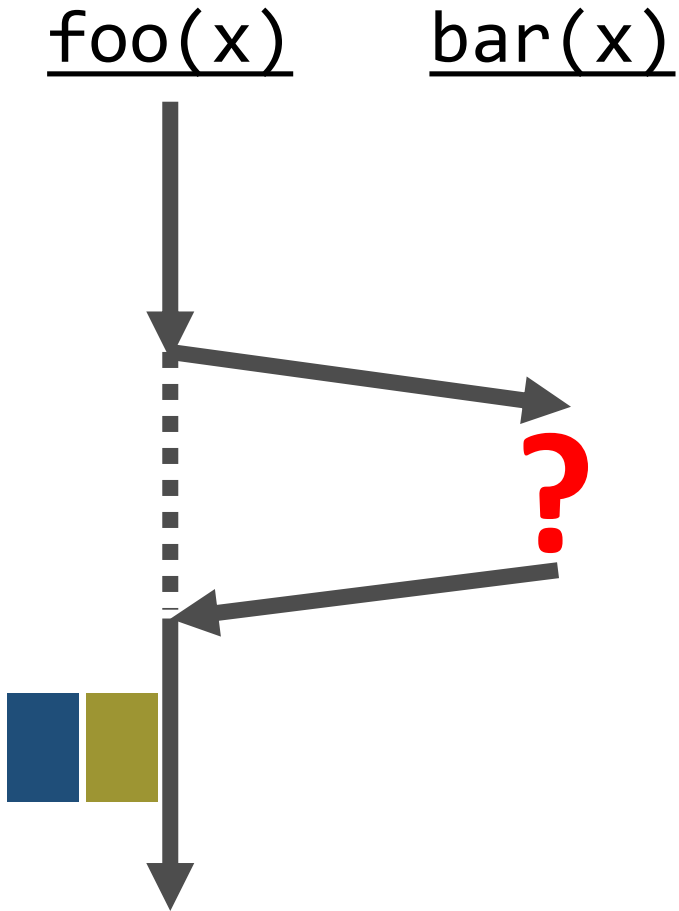
bar(x)



# Permission Transfer



# Permission Transfer

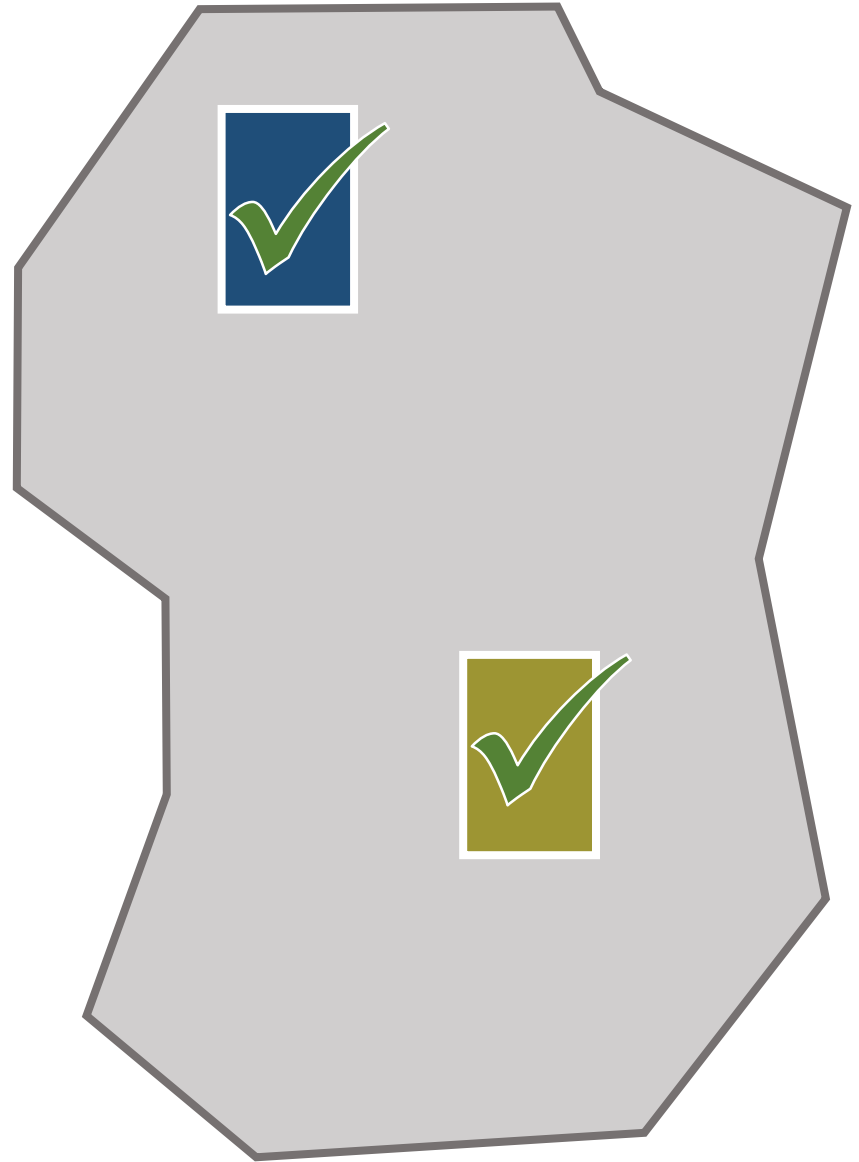




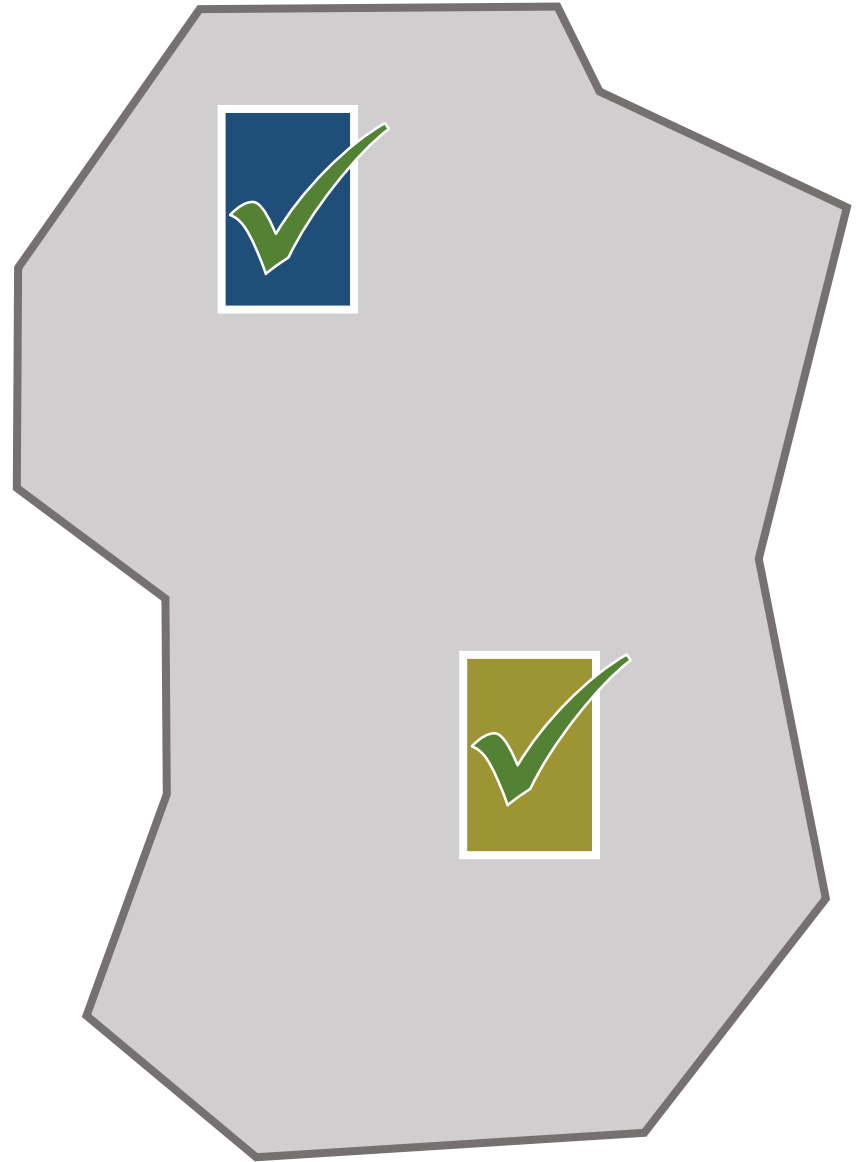
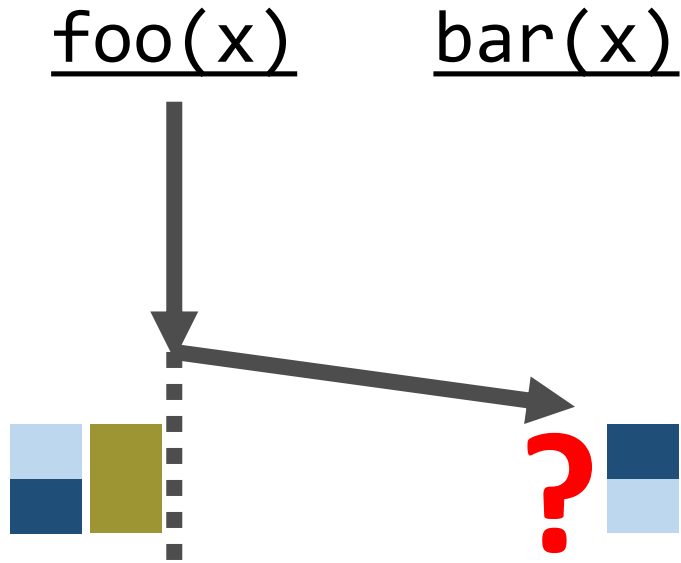
# Fractional Permissions

foo(x)

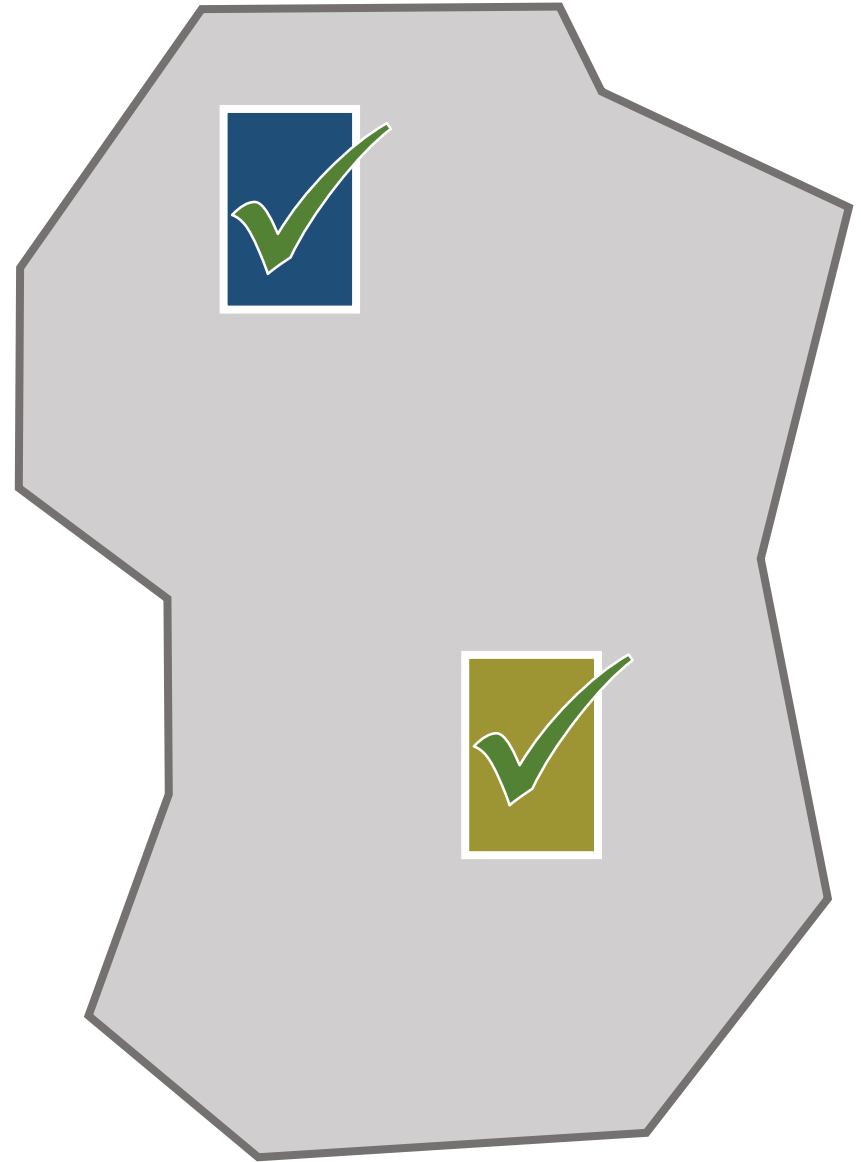
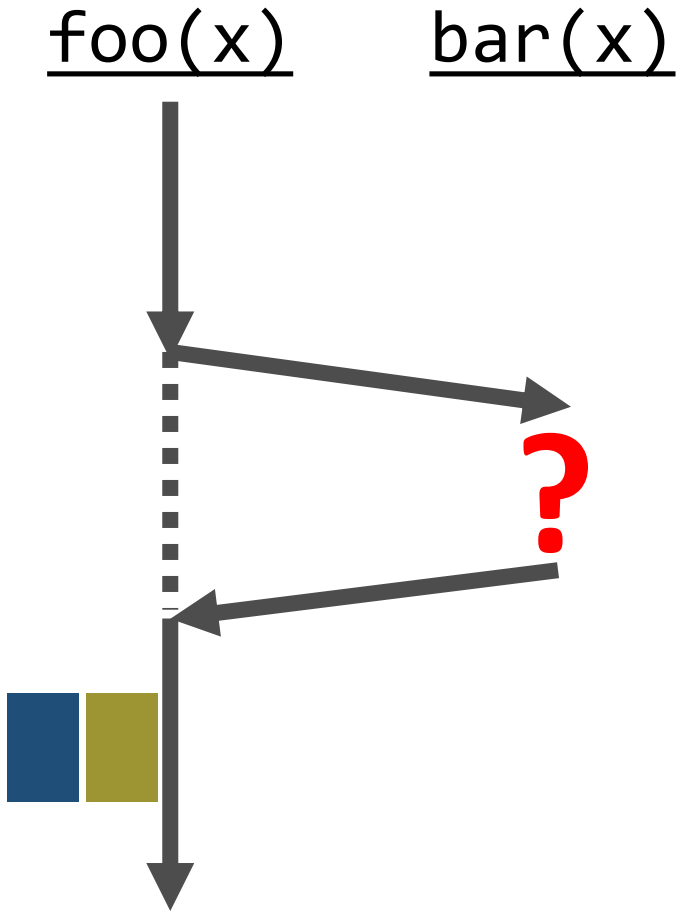
bar(x)



# Splitting Fractional Permissions



# Merging Fractional Permissions



# Silver: Assertion Language Basics

*Accessibility predicates* denote permissions

```
acc(c.f)
```

Assertions may be *heap-dependent*

```
acc(c.f) && c.f == 0
```

*Fractional permissions*

```
acc(c.f, 1/2)
```

Conjunction *sums up* permissions  
(similar to  $*$  in separation logic)

```
acc(c.f, 1/2) && acc(c.f, 1/2)
```

*Write permission is exclusive*  
(similar to  $*$  in separation logic)

```
acc(c1.f) && acc(c2.f, ε)  
⇒ c1 != c2
```

# Demo

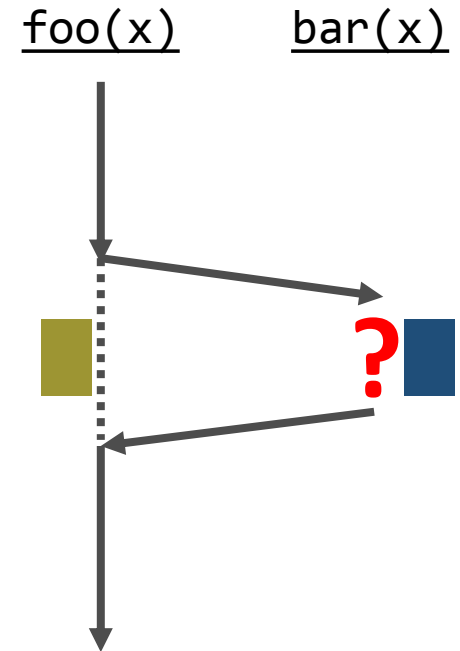
# Permission Transfer Reloaded

Idea of *permission transfer* generalises

- Fork-join (transfer between threads)
- Locks (transfer to/from lock invariant)
- Message passing (pass permissions)

Common operations

- **Gain** permissions
- **Lose** permissions



# Silver: Inhale and Exhale Statements

Statement **inhale** **A** means

- Gain permissions required by **A** (e.g. `acc(x.f)`)
- Assume logical constraints in **A** (e.g. `x.f != 0`)

Statement **exhale** **A** means

- Assert and remove permissions required by **A**
- Assert logical constraints in **A**
- Havoc locations to which all permissions were removed (i.e. forget their values)

# Concurrency Examples



# Fork-Join Concurrency (Pseudo-Java)

---

```
class Cell {  
    int v  
  
    void add(Cell c) {  
        v = v + c.v  
    }  
}
```

---

```
void client() {  
    Cell c1 = new Cell()  
    c1.v = 1  
    Cell c2 = new Cell()  
    c2.v = 2  
  
    Token tk = fork c1.add(c2)  
    // ...  
    join tk  
  
    assert c1.v == 3  
    assert c2.v == 2  
}
```

---

# Locks and @GuardedBy Annotations (Pseudo-Java)

---

```
class SharedPair {  
    @GuardedBy("this")  
    int x, y
```

# Lock Invariants (Pseudo-Java)

---

```
class SharedPair {  
    @GuardedBy("this", "x < y")  
    int x, y
```

```
}
```

---

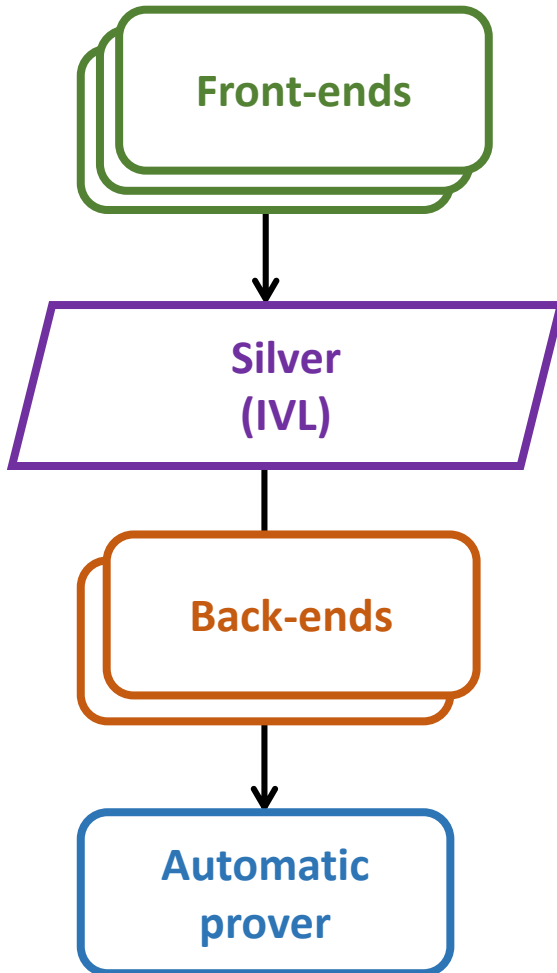
# Lock Invariants (Pseudo-Java)

---

```
class SharedPair {  
    @GuardedBy("this", "x < y")  
    int x, y  
  
    void inc(int dx, int dy) {  
        assert dx <= dy  
        synchronized(this) {  
            assert x < y  
            x = x + dx  
            y = y + dy  
            assert x < y  
        }  
    }  
}
```



# Viper: Our Verification Infrastructure



## Silver:

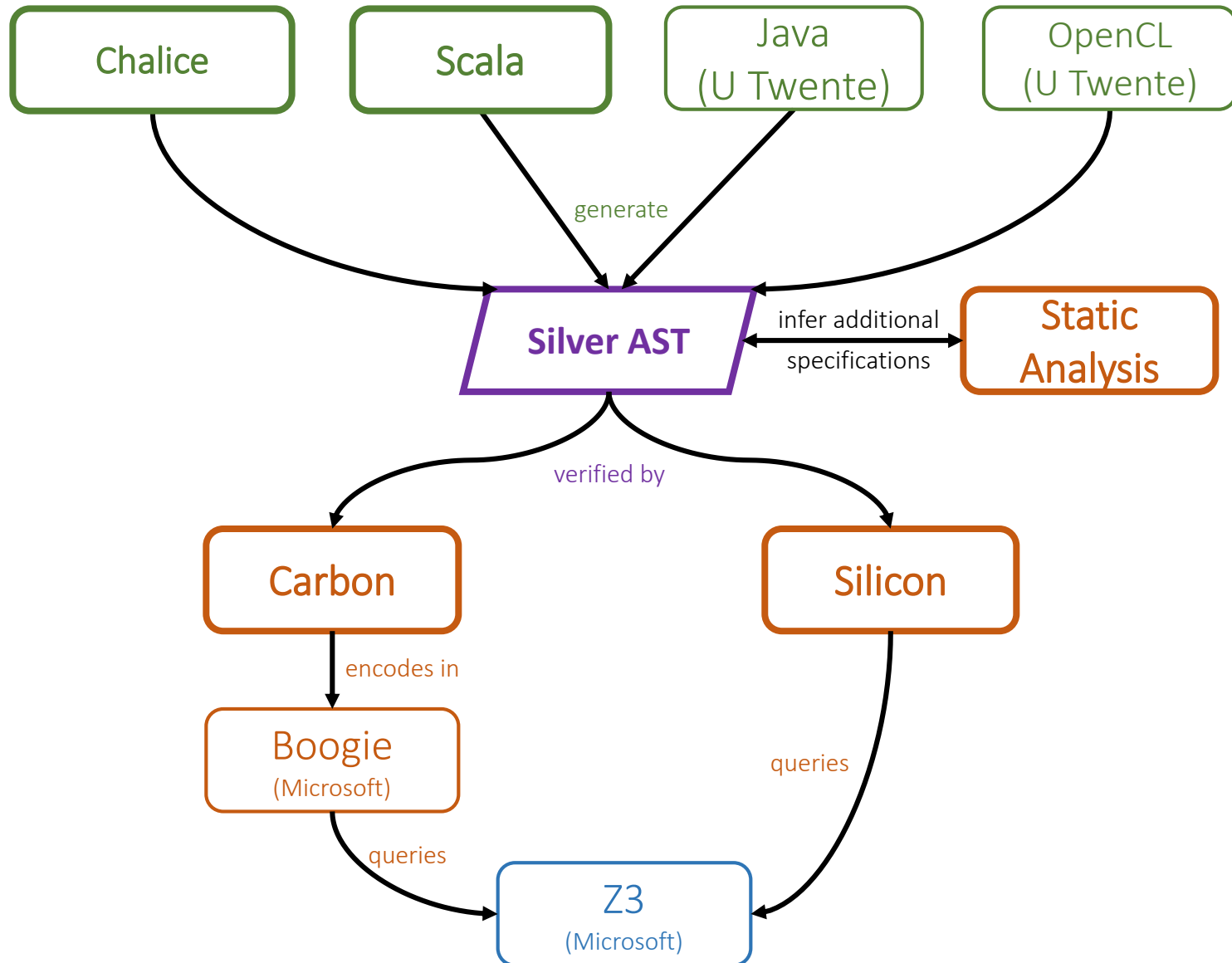
- Intermediate Verification Language
- Few (but expressive) constructs
- Designed with verification and inference in mind

**Back-ends:** Two verifiers; plans to develop inference, slicer

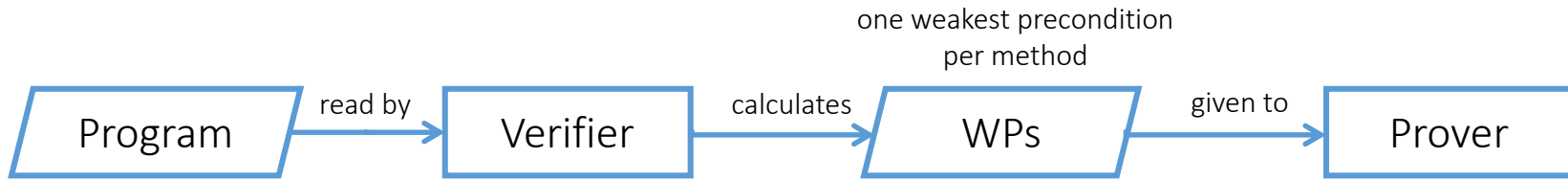
## Front-ends (proof of concept):

- *Chalice* (concurrency research)
- *Scala* (very small subset)
- *Java* (VerCors, U Twente)
- *OpenCL* (VerCors, U Twente)

# Viper: Our Verification Infrastructure

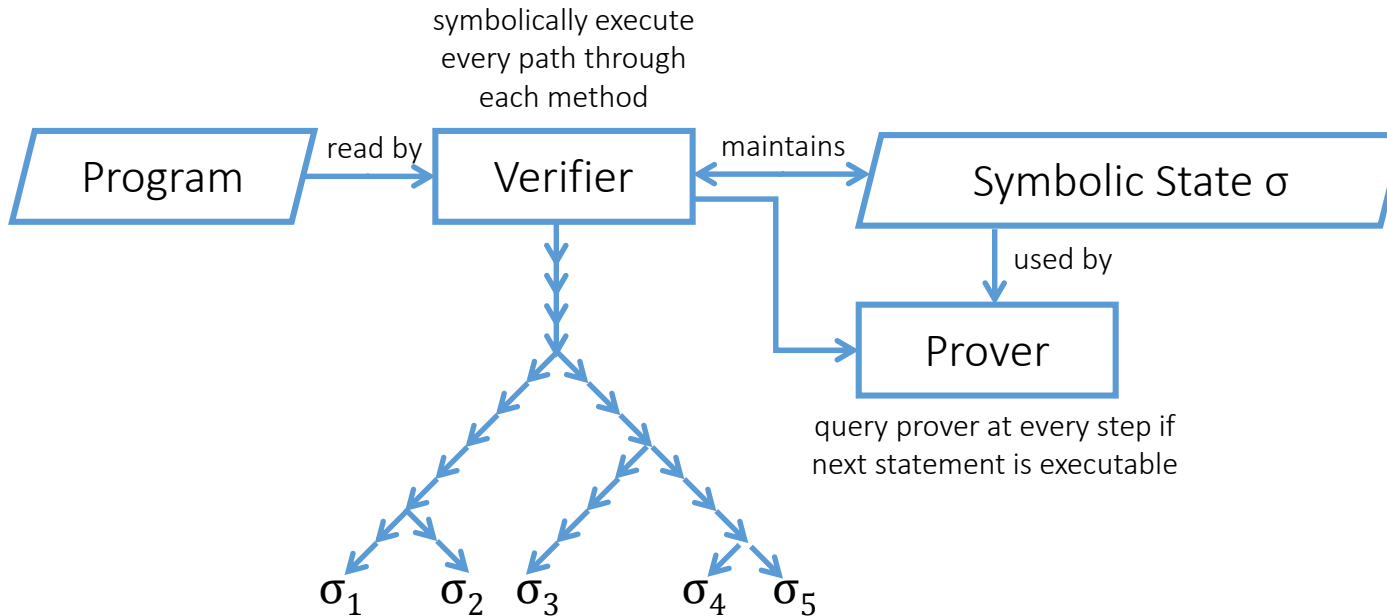


# Verification Condition Generation vs. Symbolic Execution



VCG

Query prover once with full information (Carbon)



SE

Query prover often with limited information (Silicon)

# Outlook

Information hiding, abstraction and inheritance

Unbounded (recursive) data structures

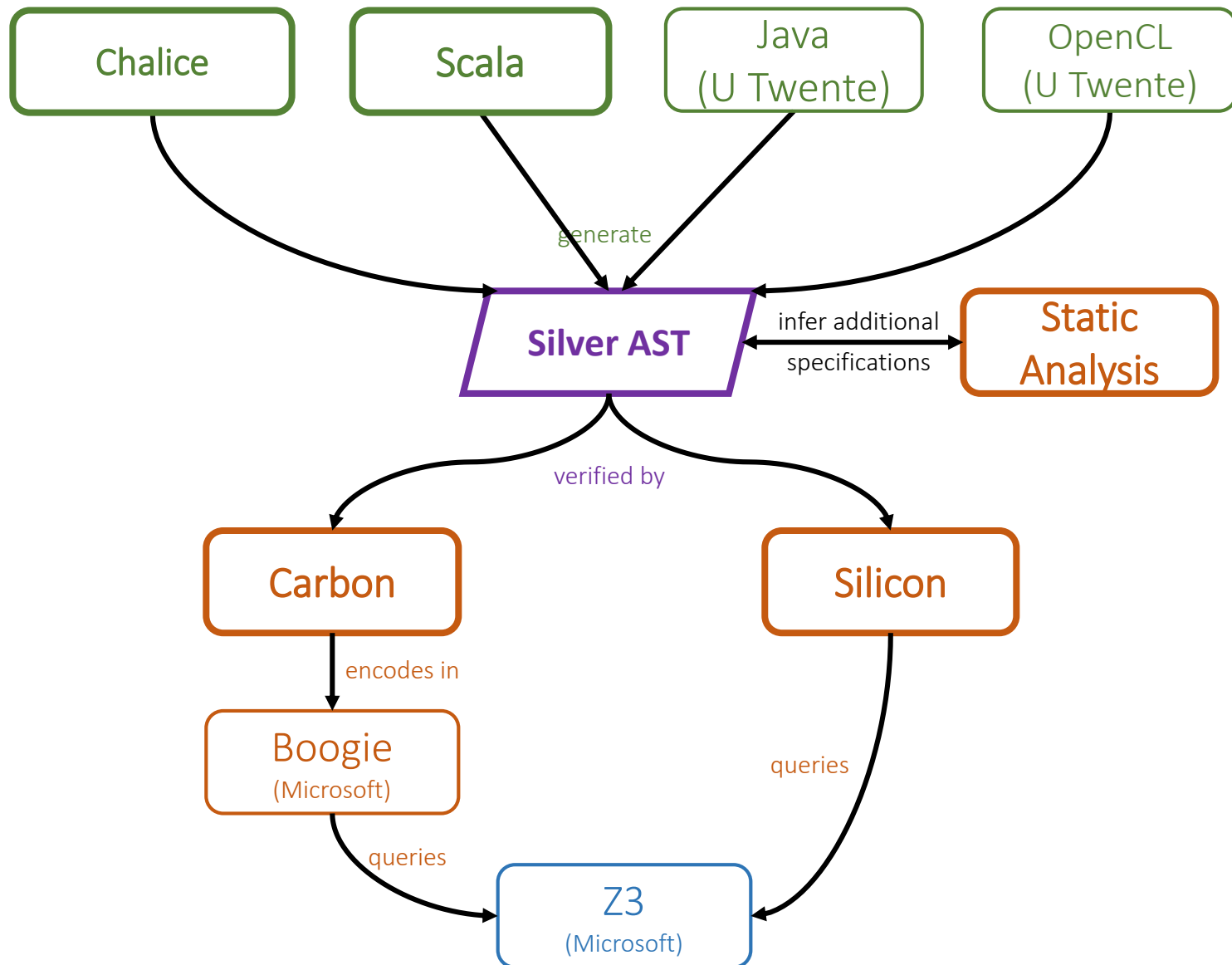
Obligations – the dual to permissions

Specification inference

Encoding of high-level features

- Immutable data (vs. permissions)
- Lazy evaluation (vs. permissions)
- Closures/higher order functions
- Actor-based concurrency
- Fine-grained locking, lock-free algorithms





**You shouldn't even be  
here!**

# Fork-Join Concurrency (Pseudo-Java)

---

```
class Cell {  
    int v  
  
    void add(Cell c) {  
        v = v + c.v  
    }  
}
```

---

```
void client() {  
    Cell c1 = new Cell()  
    c1.v = 1  
    Cell c2 = new Cell()  
    c2.v = 2  
  
    Token tk = fork c1.add(c2)  
    // ...  
    join tk  
  
    assert c1.v == 3  
    assert c2.v == 2  
}
```

---

# Fork-Join Concurrency (Silver)

---

```
field v: Int

method add(this: Ref, c: Ref)
  requires acc(this.v) && acc(c.v, ½)
  ensures  acc(this.v) && acc(c.v, ½)
  ensures  this.v == old(this.v) + old(c.v)
{
  this.v := this.v + c.v
}
```

# Locks and @GuardedBy Annotations (Pseudo-Java)

---

```
class SharedPair {  
    @GuardedBy("this")  
    int x, y
```

# Locks and @GuardedBy Annotations (Silver)

---

```
field x: Int
```

```
field y: Int
```

```
define inv(this) acc(this.x) && acc(this.y)
```

# Lock Invariants (Pseudo-Java)

---

```
class SharedPair {  
    @GuardedBy("this", "x < y")  
    int x, y
```

```
}
```

---

# Lock Invariants (Pseudo-Java)

---

```
class SharedPair {  
    @GuardedBy("this", "x < y")  
    int x, y  
  
    void inc(int dx, int dy) {  
        assert dx <= dy  
  
        synchronized(this) {  
            assert x < y  
  
            x = x + dx  
            y = y + dy  
  
            assert x < y  
        }  
    }  
}
```





# Lock Invariants (Silver)

---

```
field x: Int  
field y: Int
```

```
define inv(this)    acc(this.x) && acc(this.y)  
                   && this.x <= this.y
```